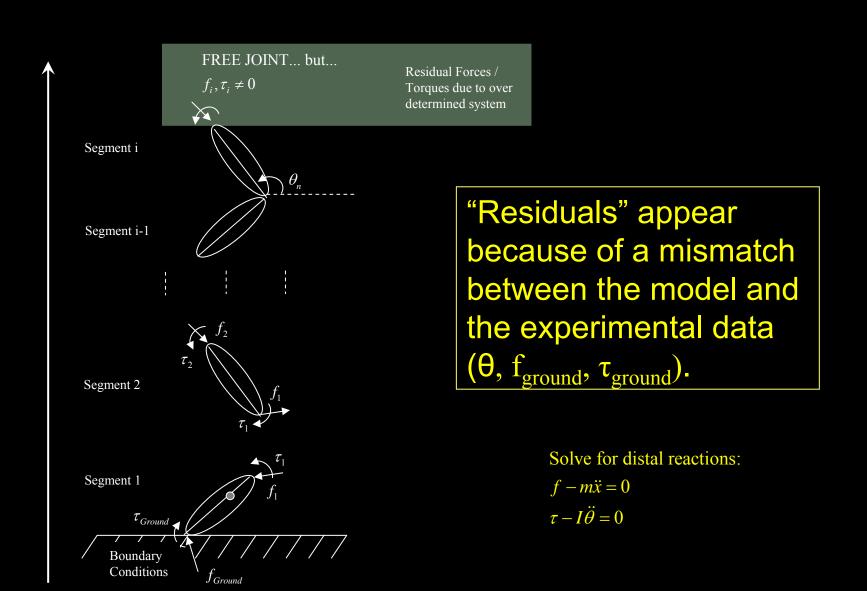


Inverse Dynamics

Solved algebraically from the ground up: NO FORWARD INTEGRATION



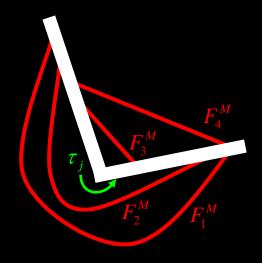
Are "residuals" bad?

YES: "Residuals" do not occur in reality: our motion is fully actuated by torques (via muscles) at the joint and NOT by the "hand of god".

We acknowledge that our experimental data contains errors (e.g. noise, skin artifact). We also acknowledge that our models are not perfect. "Residuals", therefore represent these lumped unmodeled phenomenon / errors. Having zero "residuals" would mean that we are modeling our subject perfectly and with perfect experimental data, which is highly unlikely.

Static Optimization

Solved independently at each time step: NO FORWARD INTEGRATION



solve for: $\mathbf{a} = \mathbf{a}^{\mathbf{M}}$

by minimizing: $J(\mathbf{a}) = \sum_{i=1}^{nm} (a_i^M)^2$

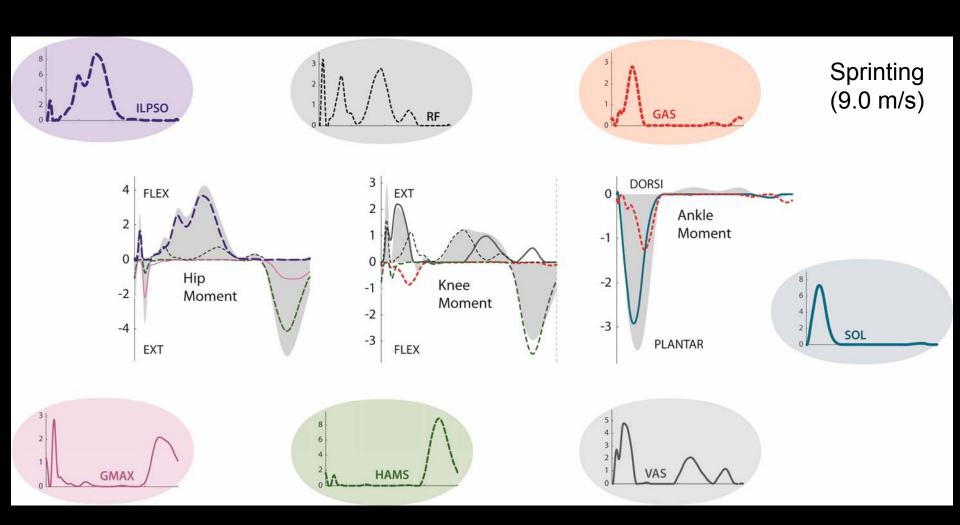
More muscles than joints: over-determined problem

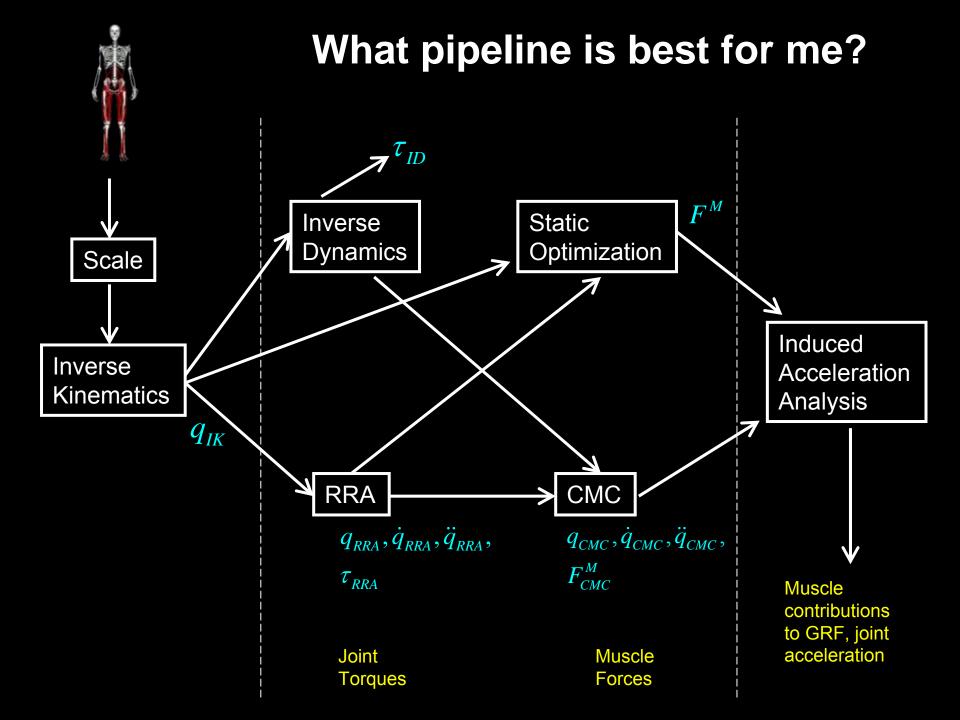
subject to:
$$\sum_{j=1}^{nj} \sum_{i=1}^{nm} \left[\underbrace{a_i^M \cdot F_{o,i}^M \cdot f\left(l_i^M, v_i^M\right)}_{active} + \underbrace{F_{p,i}^M}_{passive} \right] \cdot MomArm_{i,j} = \tau_j$$

$$\mathbf{0} < \mathbf{a}^M < \mathbf{1}$$

Static Optimization

Joint moments are resolved into individual muscular torques





	Inverse Dynamics	RRA
Forward integration	NO	YES
Tracks experimental kinematics	NO	YES
Activation & contraction dynamics	NO	YES
Time to execute	~10 sec	~5 mins
Experimental ground force applied to foot	YES	YES
Control over "residuals"	NONE	Can reduce residuals at the expense of modifying kinematics

	Static Optimization	CMC
Forward integration	NO	YES
Tracks experimental kinematics	NO	YES
Activation & contraction dynamics	NO	YES
Time to execute	~2 mins	~30 mins
Experimental ground force applied to foot	YES	YES
Time dependant objective function	NO	NO
Objective function used distribute muscle force	min(a²) across all muscles at each time step	min(a²) across all muscles at each time step

CMC Versus Static Optimization



JOURNAL OF BIOMECHANICS

Journal of Biomechanics 34 (2001) 153-161

www.elsevier.com/locate/jbiomech www.JBiomech.com

1999 ASB Pre-Doctoral Award

Static and dynamic optimization solutions for gait are practically equivalent

Frank C. Anderson^{a,*}, Marcus G. Pandy^{a,b}

^aDepartment of Mechanical Engineering, The University of Texas at Austin, Austin, Texas, USA

^bDepartment of Kinesiology and Health Education, The University of Texas at Austin, Austin, Texas, USA

Accepted 3 July 2000

Institution of MECHANICAL ENGINEERS



Special Issue Article

Comparison of different methods for estimating muscle forces in human movement

Proc IMechE Part H:

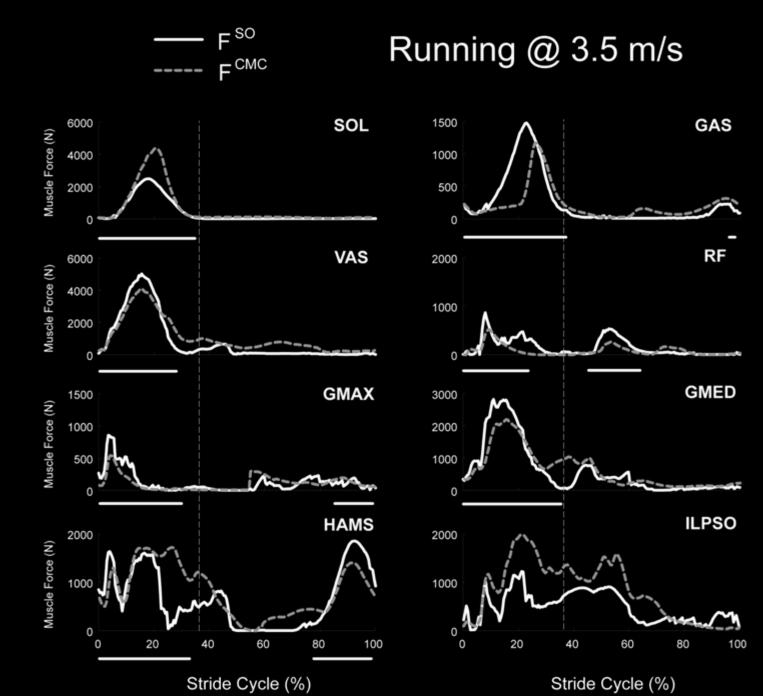
J Engineering in Medicine
226(2) 103—112

Authors 2011

Reprints and permissions:
sagepub.co.uk/journalsPermissions.nav
DOI: 10.1177/0954411911429401
pih.sagepub.com

\$SAGE

Yi-Chung Lin, Tim W Dorn, Anthony G Schache and Marcus G Pandy



Lin, Y. C., Dorn, T. W., Schache, A. G. and Pandy, M. G. (2012).
Comparison of different methods for estimating muscle forces in human movement.
Proceedings of the Institution of Mechanical Engineers Part H-Journal of Engineering in Medicine 226, 103-112.