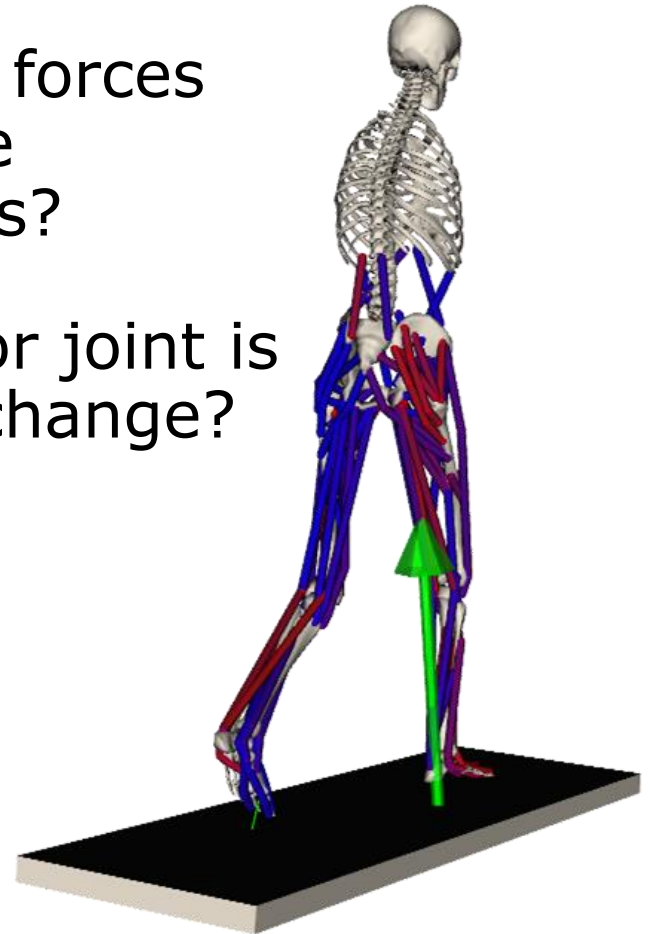


Forward Dynamics

Why Use Forward Dynamics Simulations?

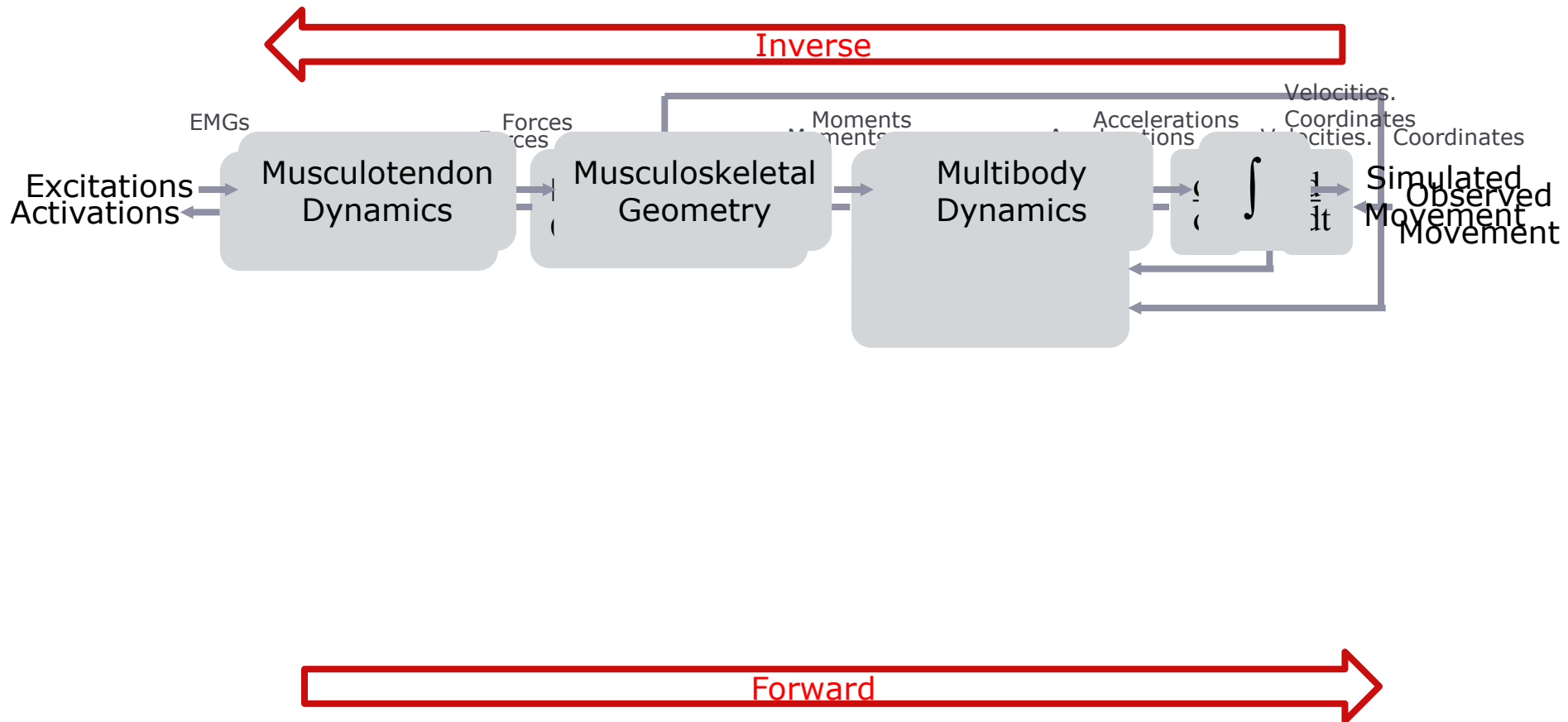
1. Validation: do forces estimated from inverse dynamics reproduce the observed motion?
2. Understanding: how do muscle forces generate motion – what are the “cause and effect” relationships?
3. Prediction: “what if” a muscle or joint is altered, how will performance change?

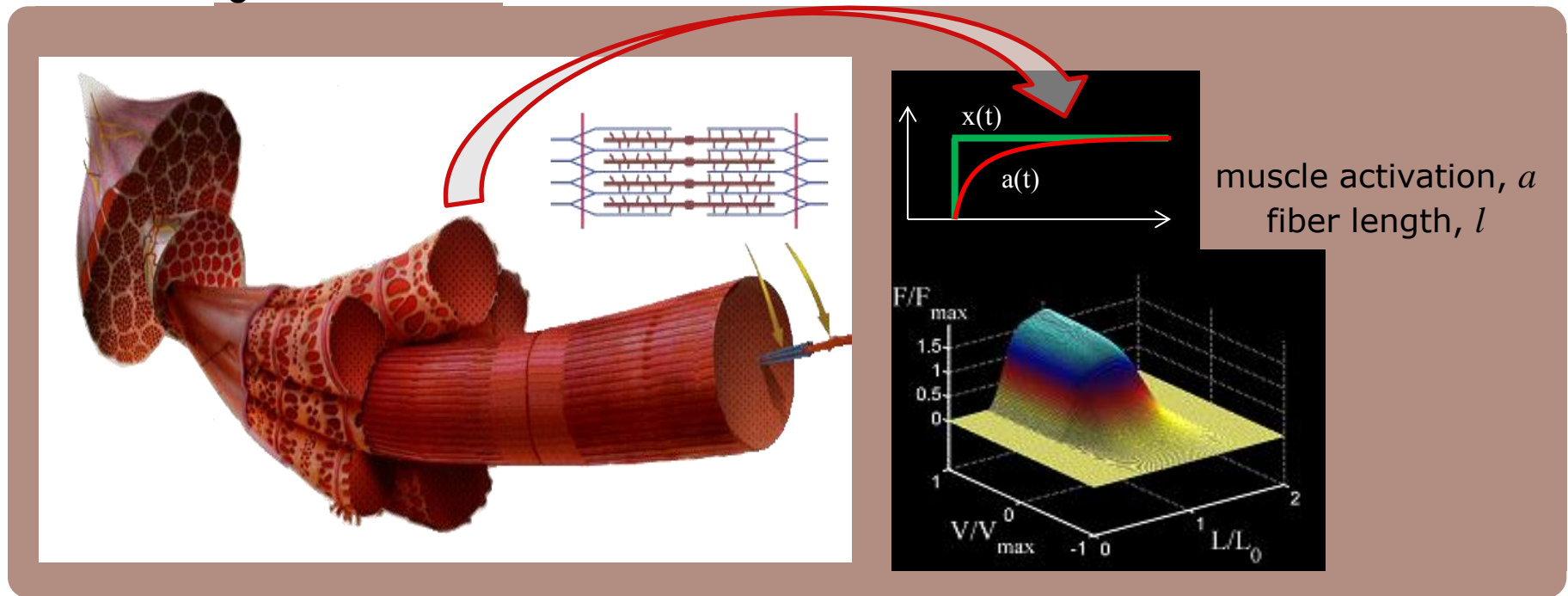
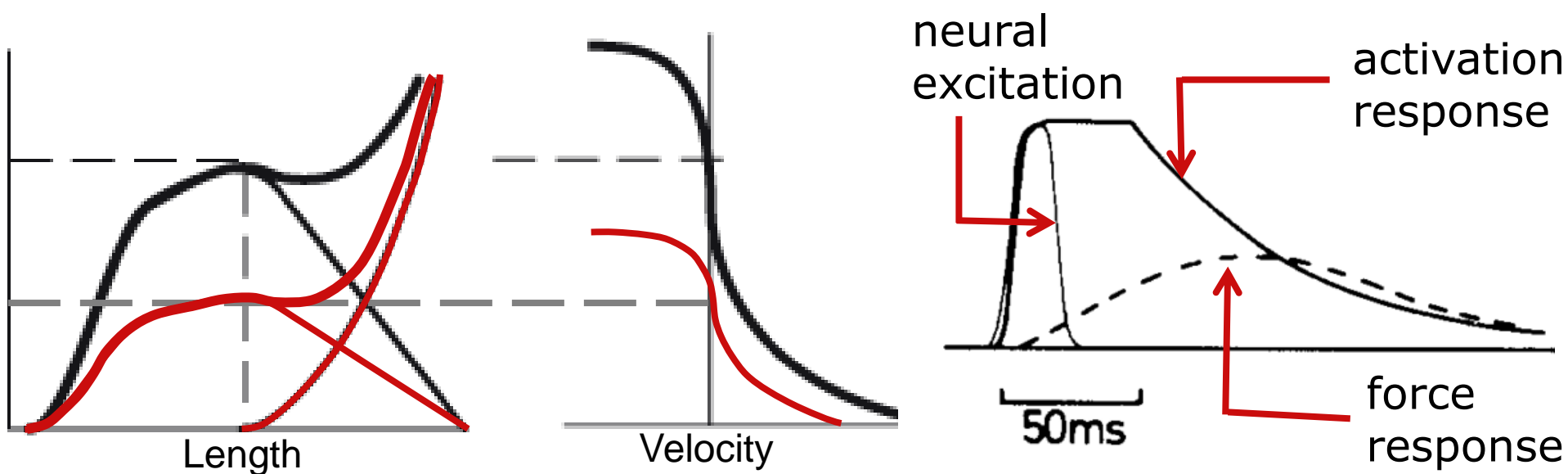


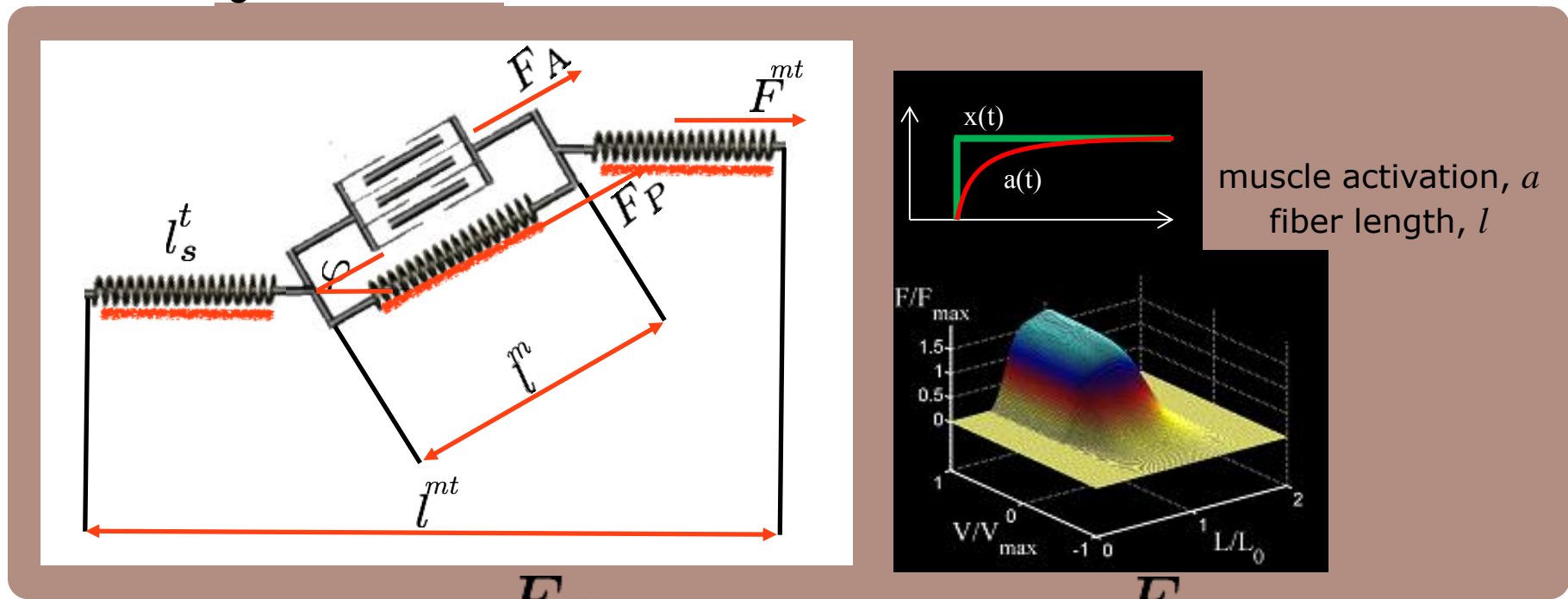
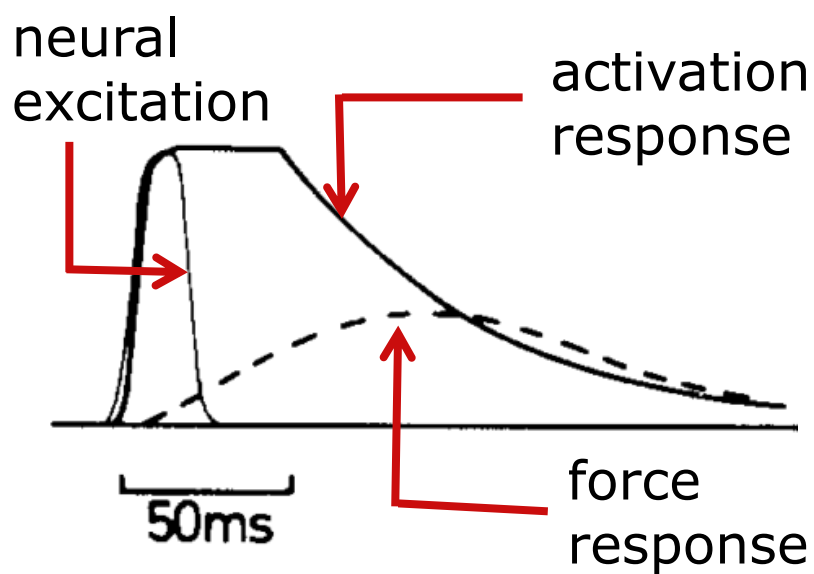
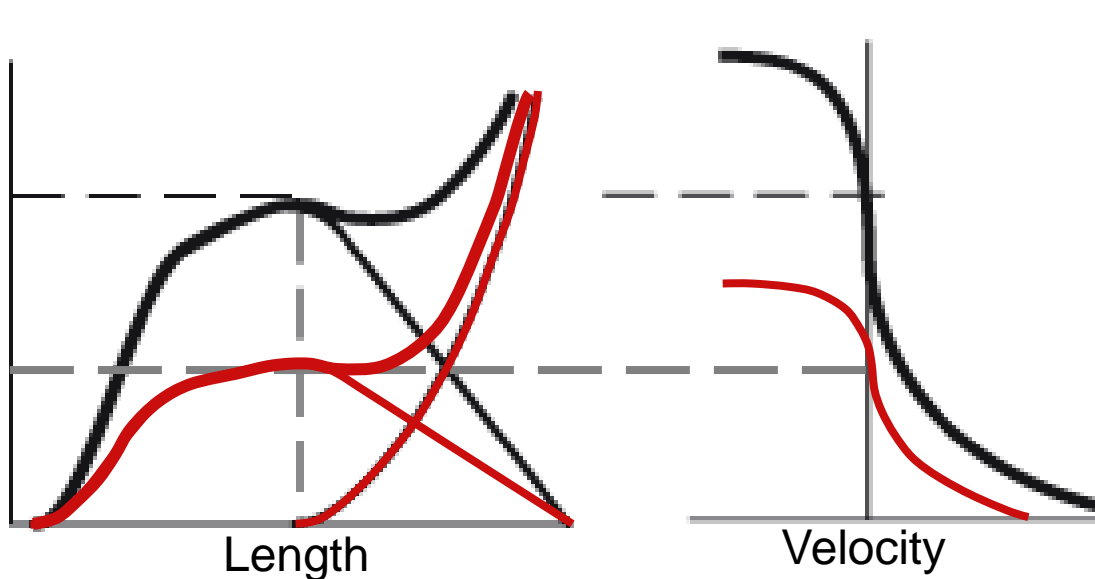
Key Concepts

- Musculoskeletal model dynamics
- States of a musculoskeletal model
- Controls of a musculoskeletal simulation
- Numerical integration of dynamical equations

Overview of Forward Dynamics

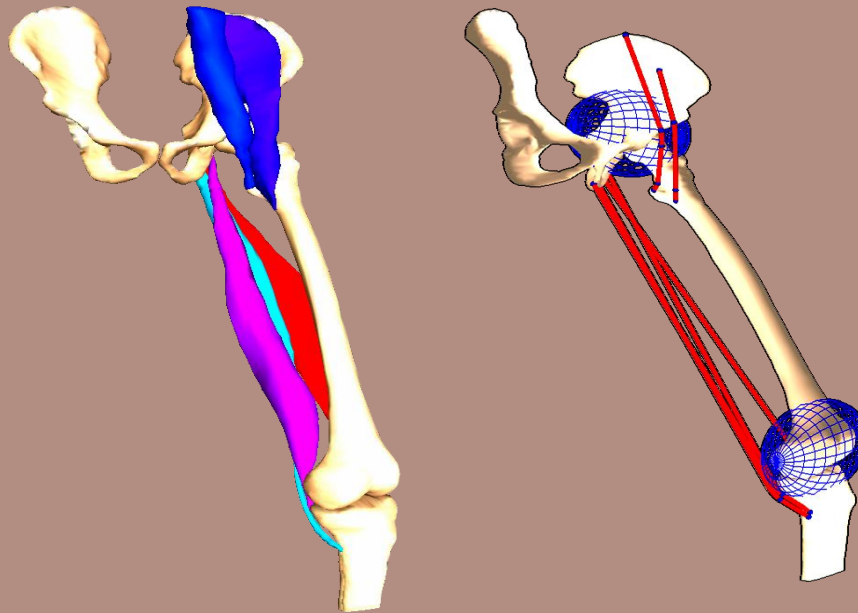
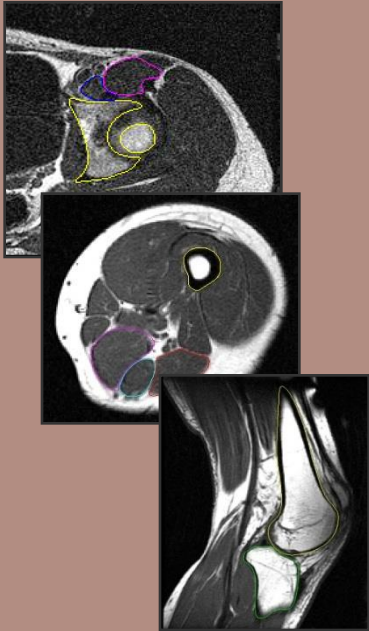
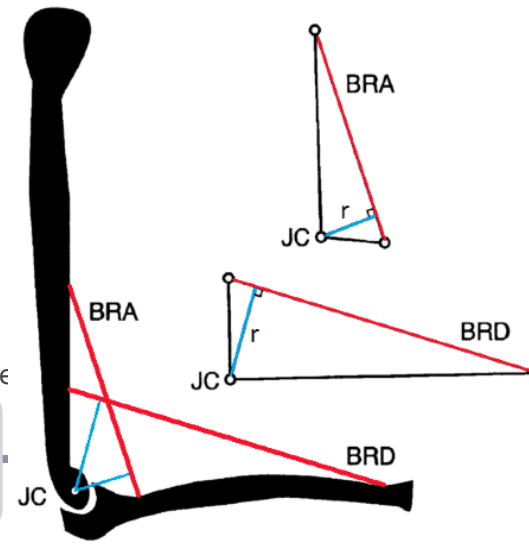
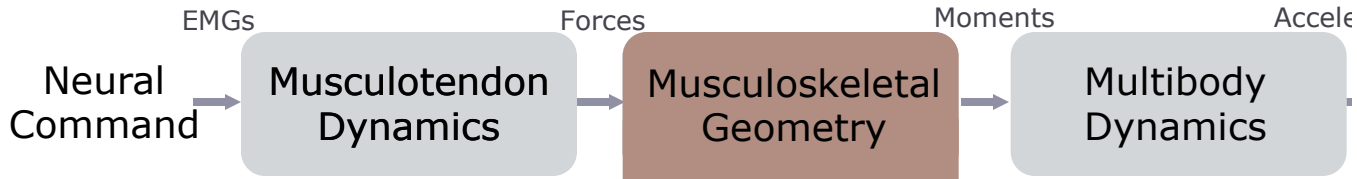






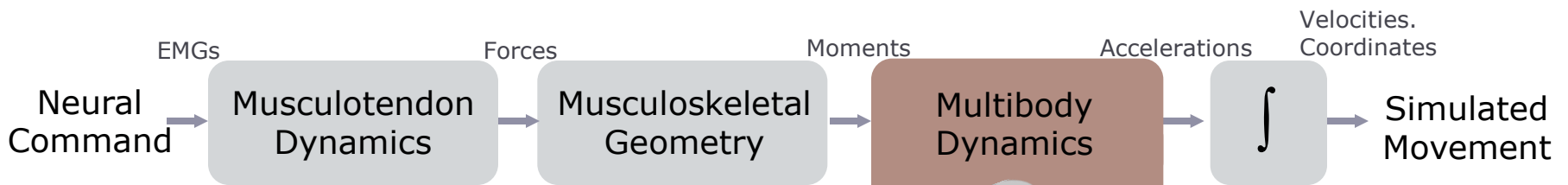
$$F^m = \underbrace{(f_A(\tilde{l}^m) \cdot f_V(v^m) \cdot a(u))}_{F_A} + \underbrace{f_P(\tilde{l}^m) + d^m \cdot \tilde{v}^m)}_{F_P} \cdot F_0^m \cdot \delta$$

Musculoskeletal Model Dynamics

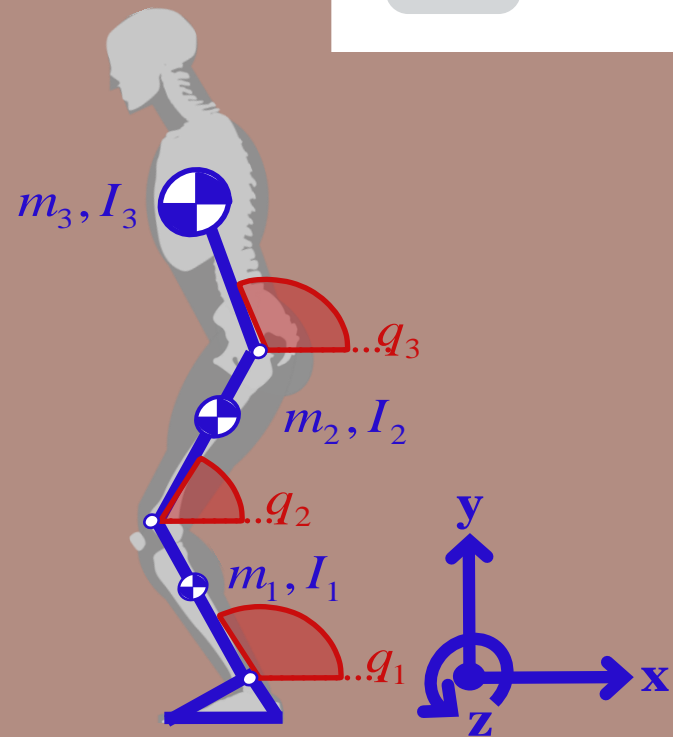


muscle lines of action
moment arms

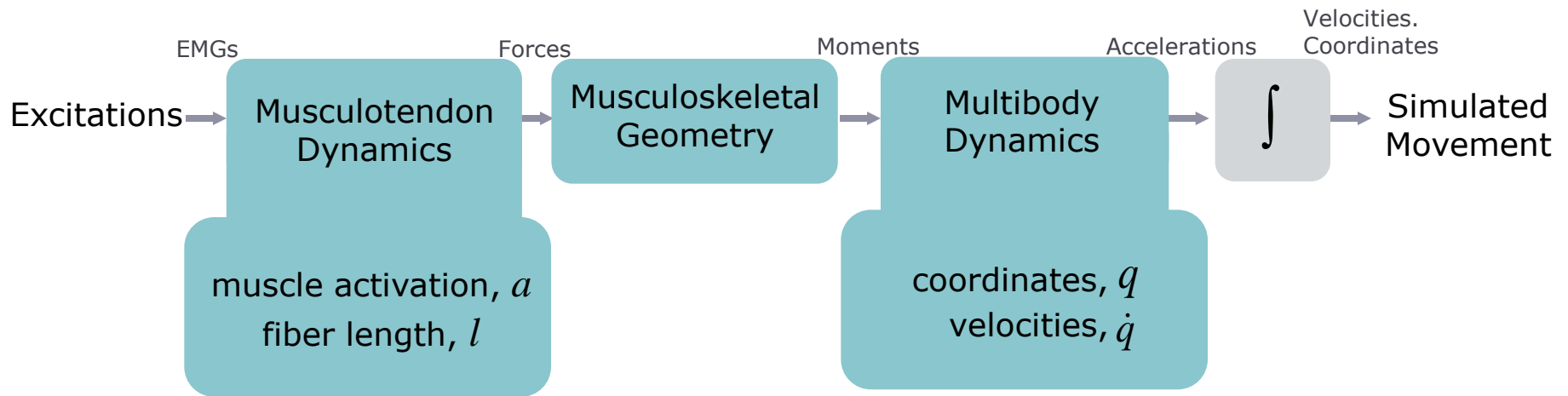
Musculoskeletal Model Dynamics



coordinates, q
velocities, \dot{q}

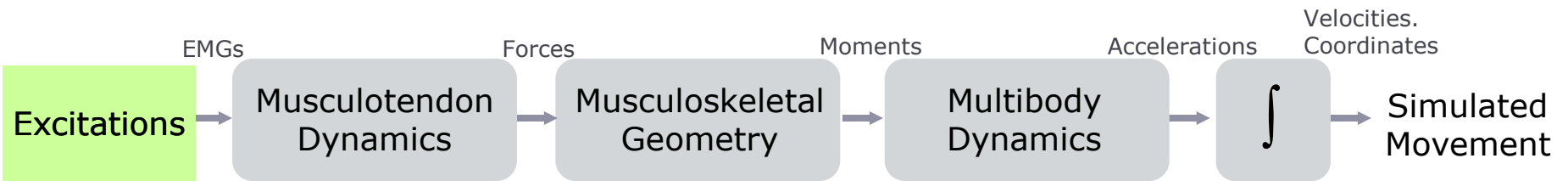


States of a Musculoskeletal Model



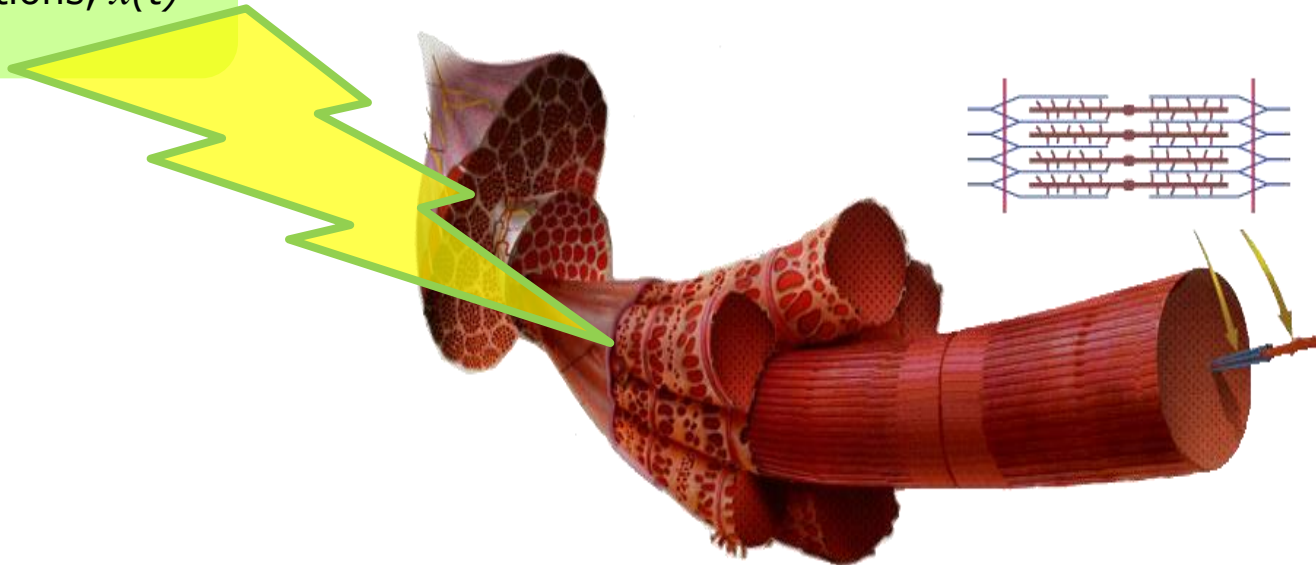
- States are model variables that are governed by the dynamics
- All measures of interest can be calculated from the states

Controls of a Musculoskeletal Model

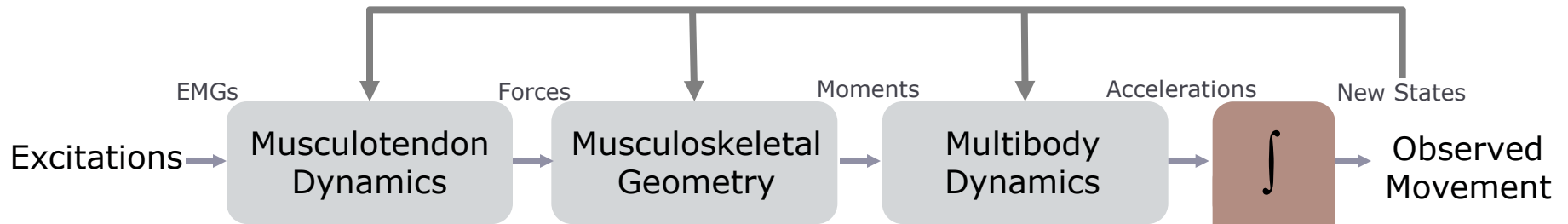


Controls

muscle excitations, $x(t)$



Numerical Integration of Dynamical Equations



Controls

muscle excitations, $x(t)$

Initial States

joint coordinates, q
joint velocities, \dot{q}
muscle activation, a
fiber length, l

Model dynamical equations:

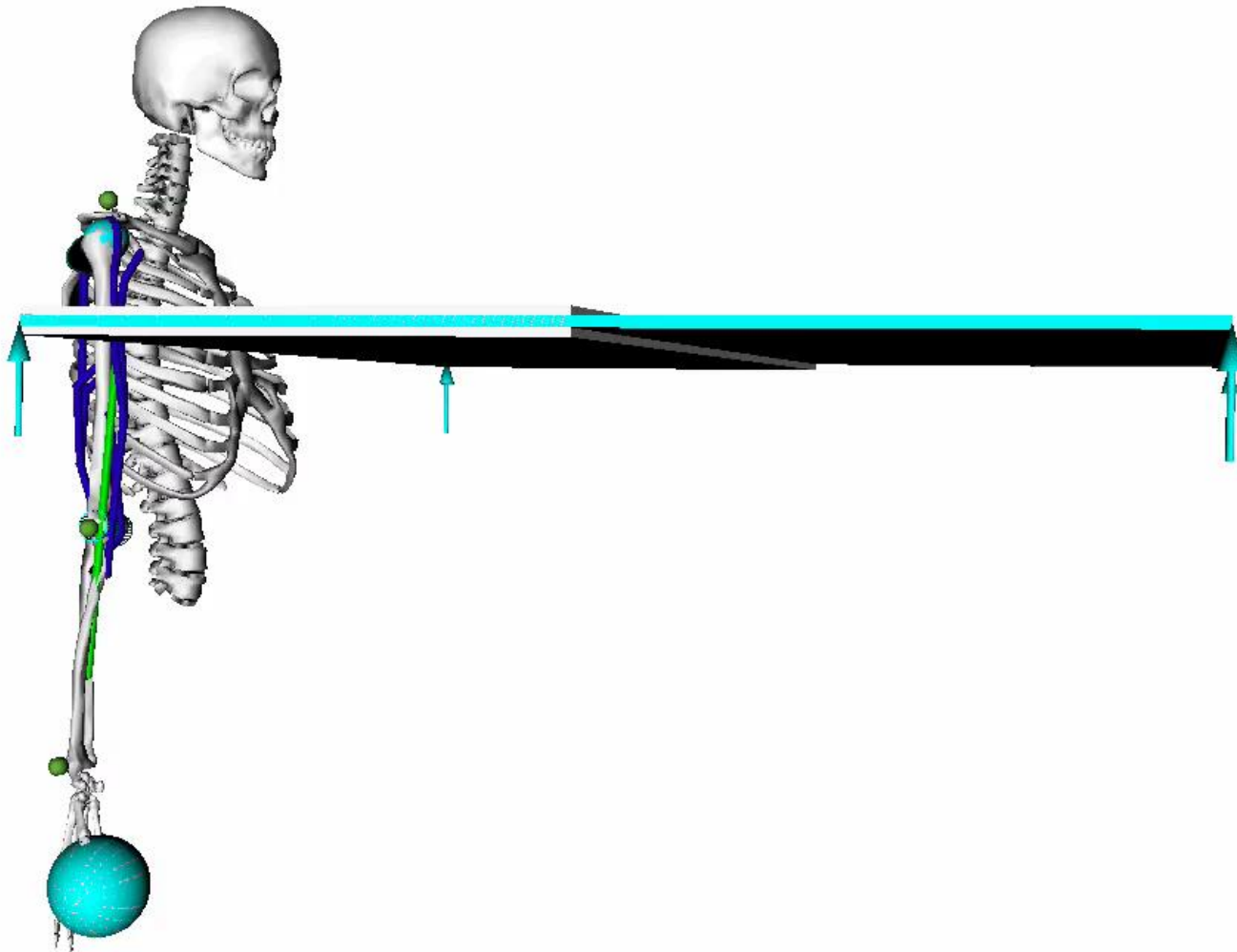
$$\ddot{q} = [\mathbf{M}(q)]^{-1} \left\{ \boldsymbol{\tau}_m(a, l, \dot{l}) - \mathbf{C}(q, \dot{q}) + \mathbf{G}(q) + F \right\}$$

$$\dot{a} = \Lambda(a, x)$$

$$\dot{l} = \Lambda(a, l, q)$$

Numerical Integrate from Initial States

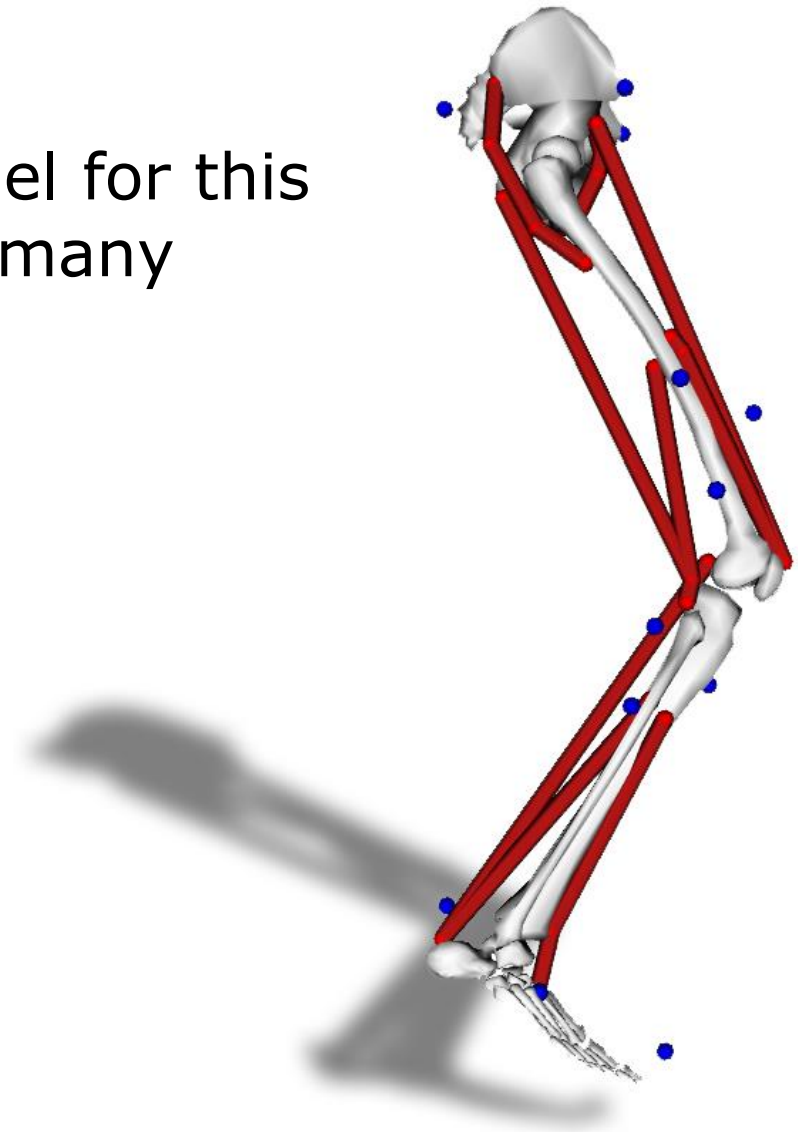
Forward Dynamic Simulation



Exercise

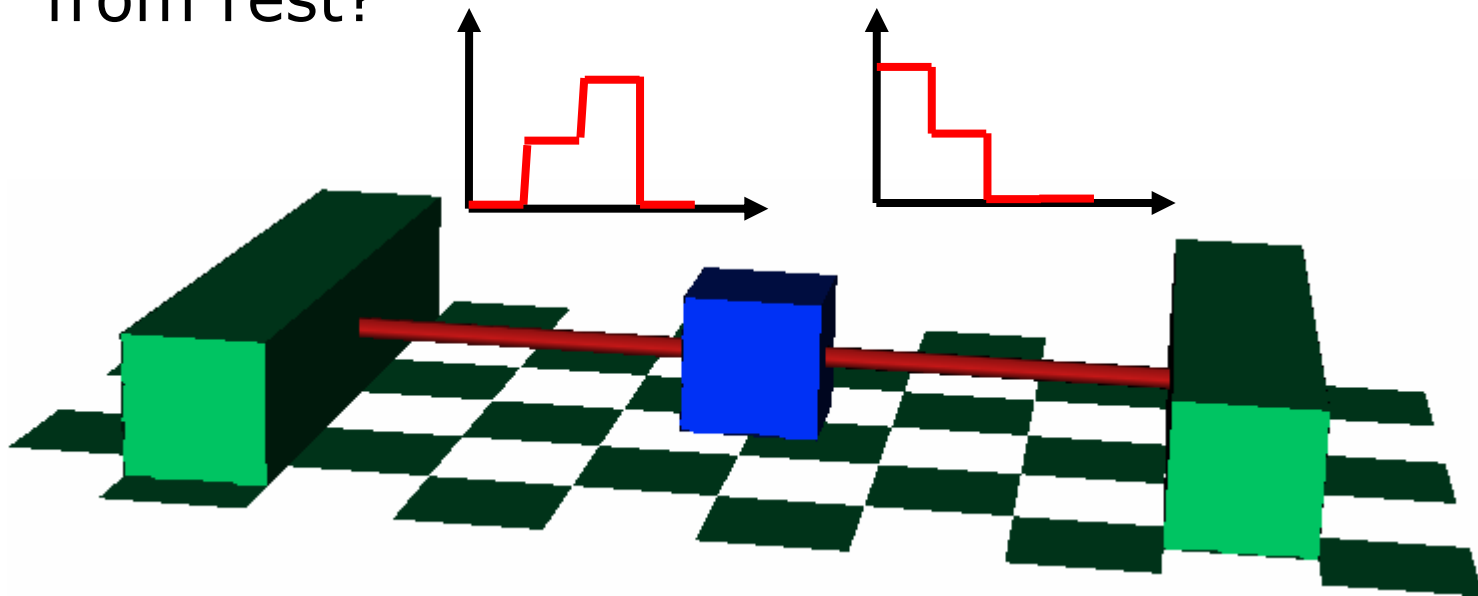
2. The musculoskeletal model for this tutorial (leg39) has how many states?

- A. 3
- B. 9
- C. 12
- D. 24



Exercise

3. Given the model below with two identical muscles and their levels of excitation plotted versus time, which way will the block initially move if starting from rest?



- A. To the left
- B. Does not move

- B. To the right
- D. Upward

Exercise

4. Given initial q and \dot{q} and muscle a and l , how are these states determined at a small instant ahead in time?
- A. Specify controls and compute \dot{a}, \dot{l} or \ddot{q} from model dynamics
 - B. Numerically integrate forces and controls from model differential equations
 - C. Numerically integrate \dot{a}, \dot{l} or \ddot{q}
 - D. Numerically differentiate forces and controls from the dynamical equations
 - E. A & C

Exercise

1. A forward dynamics simulation is
 - A. a musculoskeletal model
 - B. muscle-driven
 - C. a simulation that uses feedback
 - D. the integration of dynamical equations